# The Height Production Function from Birth to Early Adulthood<sup>∗</sup>

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#### Abstract

In this paper I specify a height production function in order to study the determinants of height from birth to early adulthood in the Philippines. I use a rich longitudinal data set on Filipino children born in 1983 and followed for more than 20 years. The structure of the production function allows height to be the result of the accumulation of inputs over time. The results show that inputs from conception to birth are relevant at each age of the children. Nutrition inputs have a positive but small effect on the child's height. The shorter the distance between the age when the nutrition input is applied and the age when height is measured, the higher the impact on height. The younger the child, the bigger the impact. The earlier disease inputs are experienced, the stronger their negative effect on height. The older the child, the stronger the effects of past diseases.

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# 1 Introduction

Starting in the 1970s, anthropometric measures have increasingly been used in the social sciences as indicators of social well-being. The seminal works for the analysis of the trends in physical stature and net nutritional status are those coordinated by Robert W. Fogel. They follow the hypothesis of the physician Thomas McKeown who claims that improvements in nutrition, hygiene and general living conditions were the principal causes of the reduction in mortality in the seventeenth to the nineteenth century. Since then, adult height has been considered an indicator of the general health status in life, of the relative risk of survival, and labor productivity (Fogel, 1986). The reason is that adult height, which does not change substantially from about age 25 to 55, is a "bridge" between living conditions in early life and health later in life (Schultz, 2005). In particular, height-for-age reflects the accumulation of past outcomes, and thus it is a long-run measure of nutritional and health status (Falker and Tanner, 1986). The early childhood investments, basically early nutrition and childhood living conditions, affect the growth of the person (Schultz, 2002). Consequently, the stock of health human capital achieved in adulthood has an impact on productivity. Finally, adult height may predict late-life morbidity and mortality through health in childhood (Bozzoli et al., 2009) and also mental health at older ages (Case and Paxson, 2008a).

Besides being considered an indicator of health status, adult height has been found to be positively correlated with earnings and labor productivity. In a recent paper, Case and Paxson (2008b) explain this result by showing that height is positively associated with cognitive ability. Using data from the United States and the United Kingdom, they document that taller children have higher average cognitive test scores and that these test scores explain a large portion of the height premium in earnings. This is due to the fact that a child's height is associated with the economic status of the family through a combination of genetic and environmental factors. Both cognition and height are driven by early childhood investments and therefore cognitive achievements are correlated with height, and wages are affected by cognitive skills (Strauss and Thomas, 2008). Poor health can explain both low height and low labor productivity. This is more evident in developing countries where living conditions are poor (Thomas and Strauss, 1997, 1998; Steckel, 1995; Haddad and Bouis, 1991). According to the World Health Organization, in 2009, at a global level, about 178 million children are stunted, resulting from diseases, and a lack of food, vitamins and minerals. As growth slows down, brain development lags and stunted children learn less. Stunting rates among children are highest in Africa and Asia. In south-central Asia  $41\%$  of children are affected. Steckel (2009) points out that severe malnutrition retards growth and may lead to permanent stunting. Maluccio, Hoddinott, Behrman, Quisumbing, Martorell, and Stein (2009) demonstrate that early childhood nutrition is causally linked to intellectual human capital in adulthood in the form of cognitive skills.

It is therefore necessary to investigate the factors driving height, since understanding the determinants of height is important in order to understand health (Deaton, 2007). The determinants of height can be divided into environmental factors, genetic factors and the age when height is measured (Schultz, 2002). The principal environmental factor is net nutrition. Net nutrition is the difference between food intake and the losses to activities and to diseases, most frequently diarrheal diseases, but also fevers or respiratory infections (Bozzoli et al., 2009). In developed countries there is evidence that genetic factors explain 80% of the variation in adult height and the rest is due to environmental factors. The proportion of the variation due to genetics seems to be less important when environmental stress is strong (Silventoinen, 2003). In developing countries environmental factors are more important for growth than in developed countries if one thinks about the lack of nutrition and the diffusion of many diseases. The age when height is measured must also be considered. In fact, most of the common historical and modern evidence looks at adult height (Steckel, 2009). However, human growth spans approximately 20 years, from conception to maturity, with the critical periods of infancy and adolescence in between. Comparing the same population over time, the age at which adult height is attained varies (A'Hearn et al., 2009). This is also true between developed and developing countries. Deaton (2008) notes that in India, people reach their adult height only in their twenties, several years later than in contemporary rich countries. Adult height is just the final result of a not-well-known process of growth that involves many different mechanisms and variables. The economic literature on height lacks studies in which individuals are followed from conception to maturity.

In this paper I estimate a height production function from birth to maturity, covering the entire human growth path. To motivate the specification of a production function, I follow Steckel (2009) reasoning:

It is useful to think of the body as a biological machine, which consumes food as fuel - a blend of calories, protein, micronutrients and other ingredients. This machine expends fuel to breathe, keep warm, circulate the blood and so forth, and in physical effort, fighting infection and physical growth. The body's first priority is to survive, and growth stagnates or takes a back seat under conditions of inadequate net nutrition. If good times return, the body may recover much or all of foregone growth through a process of catch-up, whereby velocity exceeds that typical for a given age... (Steckel, 2009)

Similar to the production process of a firm, the body can be considered a machine that combines different inputs through a particular technology to produce an output that in this case is height.

The reason for estimating a production function is to find the ceteris paribus

effects of each of the inputs. If I consider calories intake and diarrhea as two of the inputs, the questions to answer are: "How does an exogenous change in caloric intake, holding all other inputs constant, affect height?". "How does an exogenous change in diarrhea episodes, holding all other inputs constant, affect height?" And "At which age are those changes more relevant?"

Todd and Wolpin (2003, 2007) use a simple model of achievement to explain the data and the economic theoretical requirements needed to estimate a cognitive skill production function. My intention is to find the technological parameters that answer the previous questions. Therefore, I apply the same approach as in Todd and Wolpin (2003) to the case of height formation. They underline the difference in the parameters estimated in non-experimental and experimental studies. In particular, by using non-experimental data it is possible to decompose the net impact that comes through a ceteris paribus biological effect of an input versus the indirect effects of parents' changing other inputs in response. Nevertheless non-experimental studies cannot answer questions such as "What is the total effect of an exogenous change in caloric intake on height, not holding all other inputs constant?" This type of question looks at the non-ceteris-paribus effect caused by changes in inputs. It is a direct policy question that requires an experimental study or a behavioral model of how parents make decisions about the inputs for their child and how the child makes decisions for himself when older. Experiments do not generally estimate production function parameters, but rather policy effects.

To estimate my model I use data from the Philippines. The Cebu Longitudinal Health and Nutrition Survey, being an observational study, allows the determination of the technological parameters of the height production function. Furthermore, it is a rich longitudinal survey of a cohort of Filipino children followed from conception, in 1983-84, to 2005. This unique data also contain information about child nutrition and diseases, individuals' anthropometry and many other variables.

The data allow the derivation of a height production function, including all of the past observed inputs prior to any height measurements. Note that height results from the accumulation of several factors over time. I consider both the child's age when height is measured and the distance between the application of the input and the outcome measure as relevant elements when estimating the height production function. The technology used is very simple: a parametric linear model with a quadratic trend for age. The focus of the paper is to find the direct effects of the determinants of height. To empirically model the height production function, I rely on two specifications that impose different restrictions on the data. I keep boys and girls separate due to their different growth paths. I also consider two types of height production function: (i) the infants' production function and (ii) the adolescents' production function. I address the omitted variables problem by estimating a hybrid production function in which I include annual household income and mother's education.

The paper is organized in seven parts. Section 2 briefly reviews three areas of height studies, underlining differences and similarities with this paper. Section 3 presents the data and a detailed description of the variables used. In section 4 I develop a theoretical model for studying the process of height formation. I then present two specifications and their assumptions for empirically estimating the technology parameters of the height production function. The model is introduced after the data, because it strongly depends on the characteristics of the data set used. Section 5 describes the empirical results. In section 6, I present some robustness checks and model specification tests. Finally, some conclusions are drawn in section 7.

# 2 Contribution to the literature

This paper contributes to three areas. The first is the area of health production functions, the second regards models of human growth, and the third focuses on the determinants of height in developing countries.

## Health production functions

The Cebu-Study-Team (1992) used the same longitudinal data from the Philippines to estimate a child health production function. They analyzed four different outcomes: gestational age, weight, diarrhea and respiratory infection. They find that individual, household and community factors affect the outputs considered. Their IV estimation deals with the problem of endogenous inputs. Their paper focuses on the first year of an infant's life. I extend the analysis up to when the child is a young adult, but focus on the height outcome only.

The paper by Liu et al. (2009) also uses the Cebu data, but considers infants from birth to age 24 months. They specify a dynamic optimization model of parents' investment in their children's health and they estimate a set of parents' demand functions for health inputs in conjunction with a set of health production functions for how a child's physiological development responds to these inputs.

My model of height formation and my specifications are built on the work by Todd and Wolpin (2003, 2007) on the production function for cognitive achievement. They specify and estimate a production function for cognitive achievement to understand the home, school and racial test score gaps.

## Models of human growth

A model of human height growth is a representation of the height growth curve. Height is the accumulation of height growth increments from birth.<sup>1</sup> The aim of these models is to fit optimally the human height path, usually using only the person's age as a regressor. Many different growth models, both linear and nonlinear, have been developed since the 1940s. The large number of parameters to estimate, the poor fit in particular parts of the curve and the lack of interpretability with the biological process are known problems associated with these models. Darrell Bock et al. (1973) were the first to estimate a whole growth curve from infancy to maturity. After that, Preece and Baines (1978) developed a family of mathematical functions that better describes the whole growth curve with few parameters. They also attempt to interpret the results biologically (extrapolating, for example, the age at peak height velocity, the age at take-off, etc). Shohoji and Sasaki (1987) extend the Gompertz growth model of stature, focused just on adolescence, by considering the entire life of a human being from birth to adulthood. Jolicoeur et al. (1988) develop an alternative curve to better fit human growth from origin (egg fertilization) to adulthood. Many other papers exist in the statistical and biomedical literature.

In general, the parameters of the growth models of human height include all of the factors affecting height, such as genetic and environmental factors. These models do not focus on the determinants of height. Their main purpose is descriptive or predictive. This paper aims only to identify the separate effects of the determinants of height. The similarity with this class of studies is the temporal window, since I am also looking at the process of height formation from birth to early adulthood.

## The determinants of height in developing countries

The determinants of height have been studied in several different fields, such as medicine, biology, demography and economics. In the economic literature on height in poor countries, many papers look at the effects on height of socioeconomic factors such as maternal education, income, poverty, child labor, political oppression or schooling.<sup>2</sup> My paper, instead, looks at the direct biological determinants of height carefully considering different estimation problems that arise when trying to estimate the causal effects of these determinants or inputs on health.

Many studies have focused on the effects of childhood health and nutrition on adult height at the population level (Deaton, 2007; Akachi and Canning, 2007).

<sup>&</sup>lt;sup>1</sup>In the growth literature there are studies on cross-sectional or individual measurements. The short review here considers the individual growth curves only.

<sup>2</sup>See Steckel (2009) and Silventoinen (2003) for the complete references.

They show the importance of childhood health and nutrition and confirm that birth and adolescence are critical periods. However, the evolution of height should be analyzed in an individual longitudinal framework to explain more clearly all of the mechanisms behind a person's growth.

# 3 Data

The data come from a joint project between the University of North Carolina and the University of San Carlos in Cebu, Philippines.<sup>3</sup> The Cebu Longitudinal Health and Nutrition Survey (CLHNS) is a longitudinal survey of a cohort of Filipino women who gave birth between May 1, 1983 and April 30, 1984. In particular, 33 communities or barangays were randomly selected from the metropolitan Cebu area. Of them, 17 are urban communities and 16 are rural communities. The baseline survey includes 3327 women who were interviewed during the 6th to 7th month of pregnancy. All pregnant women of the barangay and the births were identified, and 3,080 non twin live births were consequently followed in the survey. Around 2,600 households were analyzed for the first 2 years. The children who were born during that period, their mothers, other caretakers, and selected siblings were followed through subsequent surveys conducted in 1991-2, 1994-5, 1998-9, 2002 and 2005. Apart from those last surveys, bimonthly surveys were conducted after birth for 24 months. There are 18 waves in total, 13 collected during infancy and early childhood and 5 during middle childhood, adolescence and early adulthood.

The initial focus of the survey was to collect information about the infants' feeding patterns. Later on, when the children were followed through adolescence and into young adulthood, the objective changed to a longitudinal intergenerational study of health.

The survey covers issues such as health, nutrition, water quality and sanitation. It contains detailed information about the mother's health and behavior during pregnancy, such as health care practices or smoking behavior, children's education, household and individual economic situation and job, demographic information, family planning, intra-household relationships, reproductive health and sexual behaviors.

Of special interest for my study is the rich collection of anthropometric measurements from birth to age 22, as well as complete disease and nutrition information. Furthermore, I can control for what happens between conception and birth, given that I have information about the pregnancy and the pregnant mother. Since the data have information at the individual, household and community levels, it is possible to study the longterm effects of prenatal and early childhood nutri-

<sup>3</sup>For further information, go to www.cpc.unc.edu.

tion and health on later adult outcomes, matching physical and socio-economic information.

It is important to notice that individuals are not surveyed at the same age. The waves of the panel are not evenly spaced. Table 2 reports the children's age at the time of the different follow-ups. For simplicity, later on I will use the range of ages, labeling them with the round mean age. The age ranges underlined in light blue are the waves considered in the adolescent height production function, while for infants, I use the waves underlined with a star (\*).

Table 3 reports descriptive statistics for the variables considered. The values reported refer to the children at birth and when they are mean age 1, 2, 8.5 and 18.7 years. The following paragraphs include the detailed description of each variable one by one.

## 3.1 Outcome

Infant height and weight were measured every two months for the first two years of life by the field staff in Cebu. Height was measured using infantometers.<sup>4</sup> For children and teenagers, ordinary meter sticks were used to measure their height. Height is reported in centimeters, jointly with the date of measurement. I use the raw height measures.

## 3.2 Inputs from birth to age 22

The three major factors affecting the height of a person at time  $t$  are genetic factors, environmental factors (basically net nutrition), and age at the time of measurement (Schultz, 2002).

#### 3.2.1 Genetics

Many medical papers suggest that approximately 60% of height variation in a population depends on genetic factors, but it is not clear which is the underlying process (see, e.g., Ginsburg et al., 1998) nor is the relationship between genetics and environmental factors clear.

Individuals inherit both chromosomes and genes, but it is not known, for example, if the  $X$  chromosome has a bigger effect than the  $Y$  chromosome or vice versa (Carter and Marshall, 1978). DNA is inhered but height can be developed.

I do not have information about DNA and I use the mother's height as a proxy for genetics.<sup>5</sup> Subramanian et al.  $(2009)$  found a negative association between

<sup>4</sup>The infantometer is a length measurement used for infants and children who are unable to stand.

<sup>5</sup>Unfortunately, the father's height is not available in the survey.

maternal height and poor health in children (in particular, child mortality, anemia and anthropometric failure) in India. This suggests an intergenerational transfer of health from the mother to her offspring.

I assume that the rest of the genetic impact is captured by a biological endowment included in the model. It represents the genetic inheritance and geneenvironment interactions.

#### 3.2.2 Environmental factors

Caloric intake Typically, medical studies use nutrients as nutrition factors, but I include caloric intake, which is a good aggregate indicator of nutrition, even if it does not capture the role of micronutrients (Branca and Ferrari, 2002).

The energy intake for infants is exclusive of breast milk, since the Cebu Team was not able to compute calories from breast milk, given the complexity and almost impossibility of doing that.<sup>6</sup> I consider the calories from nutrients different from the calories in human milk for infants.

Daily energy intake<sup>7</sup> is calculated from 24-hour dietary recalls during the surveys from birth to 2 years and in 1994, 1998, 2002 and 2005. During the 1991-92 survey, the child's intake is based on quantitative food frequency questionnaire, with items derived from a list based on 24-hour food recalls from women in the sample.

Breast feeding Feeding patterns in the first year of life have probably the strongest impact on infant development (Morgan, 1999). Wrong timing in the introduction of a food or inadequate diet can cause development and health problems for the child.<sup>8</sup> Early lactation protects the infant from the environment both through the nutrients and the protective factors that breast milk provides. However, malnourished mothers may be unable to produce sufficient quantities of good quality milk to satisfy the baby's needs (Scott and Duncan, 2002).

<sup>&</sup>lt;sup>6</sup>The composition of human milk is not uniform and changes during the course of lactation. The greatest change in composition occurs during the first 10 days post-partum when colostrum changes to mature milk. In addition, the calories contained in breast milk depend on the mother, on her's nutrition, on the quantity of breast milk the infant sucks, and on the time of day and it also changes during a single feed (Scott and Duncan, 2002).

<sup>7</sup> I am thankful to Linda Adair who provided me with the caloric intake computed by using the Food Composition Table owned by the Food and Nutrition Research Institute in the Philippines.

<sup>8</sup>There are some standard rules for the age of weaning: the WHO recommends exclusive breastfeeding for six months, introducing age-appropriate and safe complementary foods at six months, and continuing breastfeeding for up to two years or beyond. Weaning is one of the most crucial events in a child's diet.

Besides the nutritional importance of human milk,  $9$  breastfeeding can lengthen the duration of postpartum amenorrhea and thereby delay subsequent births. In developing countries, this is a common contraceptive method.

I include a dummy variable that indicates whether human milk was given to the baby and an interaction term between breast milk and caloric intake.

Diseases In developing countries, there is clear evidence about the effect of diseases on human growth. Along with nutrition, childhood diseases are indicated to have an effect on growth. In fact, some diseases reduce the absorption of nutrients, prevent food intake, produce nutrient losses or increase metabolic requirements (Stephensen, 1999). The association between undernutrition and diseases is likely to be bidirectional. Thus, diseases not only affect nutrition, but undernutrition also predisposes to diseases (Victora et al., 1990; Walter et al., 1997).

Silventoinen (2003) lists the diseases that, in the literature, have been found to affect human growth. In particular, inflammatory diseases hinder the growth of long bones, diarrhea can lead to malnutrition, and pneumonia has been found to have similar effects on growth. Some evidence exists that diabetes and asthma could be associated with a lower growth rate, while infections may interact with nutrition and chronic diseases, including severe conditions such as congenital heart disease. All of these diseases are likely to have an influence on growth as well as on final body height.<sup>10</sup>

I distinguish between infants and adolescents because diseases have a different impact on a person, depending on age.

Infants' diseases Bozzoli, Deaton, and Quintana-Domeque (2009) and Akachi and Canning (2007) use infant mortality as a measure of disease in childhood. I prefer to look at the different diseases.

For infants, I consider diarrhea, measles and other important diseases such as dengue fever, chicken pox, TB, primary complex, and worms or other parasites. Diarrhea is commonly the result of an infection, bacterial or viral. Weaning diarrhea occurs in a background of poor sanitation, when supplement foods are introduced in addition to breast milk and the infant is exposed to new organisms. Children who constantly suffer from diarrhea are unlikely to be well-nourished (Bozzoli et al., 2009). The consequences are dehydration, malabsorption of nutrients, poor appetite and loss of nutrients. If it is severe and protracted, it can lead

<sup>9</sup>Breast milk contains several growth factors, although the physiological importance of these elements is not clear (Morgan, 1999).

<sup>10</sup>Skerry, 1994; Martorell et al., 1975; Rowland, Cole and Whitehead, 1977; Victora et al., 1990; Brush, Harrison and Waterlow, 1997; Vercauteren and Susanne, 1976; Tattersall and Pyke, 1973; Herber and Dunsmore, 1988; Thon et al., 1992; Wise, Kolbe and Sauder et al., 1992; Cole, 2000; Poskitt, 1993. For the complete list and explanation, see Silventoinen (2003).

to death. In fact it is still among the leading causes of death in early childhood in poor countries.<sup>11</sup>

Measles can cause serious complications, including blindness, encephalitis, severe diarrhea, ear infections and pneumonia, particularly in malnourished children.

I use a dummy variable that indicates whether the infant had episodes of diarrhea or other important diseases in the seven days preceding the survey or had measles in the last two months. For the baseline I instead use a dummy variable that indicates if the infant had feeding problems in the few hours after birth.

Adolescents' diseases Whereas the effects of diarrhea on infants are clear and have been used in many empirical studies, for older children they are not as clear. Thus, for adolescents I need to consider other diseases that affect height. I consider only chronic diseases, that is, diseases of long duration and generally slow progression. I consider only chronic diseases because they capture the intensity of the sickness. It could be that other reported illnesses are temporary or do not strongly affect height.

I match the historical information in the data about a child's diseases with the diseases listed by Silventoinen (2003) that have been found to negatively affect height. To do this, I refer to the International Statistical Classification of Diseases and Related Health Problems of the World Health Organization.<sup>12</sup>

In particular, I distinguish the following groups of diseases:

- 1. Certain infectious and parasitic diseases (e.g., TB, polio, dengue, measles).
- 2. Endocrine, nutritional and metabolic diseases (e.g., diabetes).
- 3. Diseases of the respiratory system (e.g., pneumonia, asthma, weak lungs, tonsilitis).
- 4. Diseases of the digestive system (e.g., ulcers).
- 5. Congenital malformations, deformations and chromosomal abnormalities (e.g., heart disease).

I create a dummy variable that indicates whether a person suffered at least one of these critical diseases. It is important to note, for example, that the disease dummy when the child is 8 years old indicates the presence of chronic illnesses that may have started years before.

<sup>11</sup>In an article published in Time magazine in October 2006, Andrea Gerlin investigates the reasons why diarrhea still kills 1.9 million children every year. He reports the WHO statistics about the leading cause of death in children under 5. The first one is pneumonia, the second is diarrhea, the third is malaria, the fourth is measles and the fifth is AIDS/HIV.

<sup>&</sup>lt;sup>12</sup>The version used is the 2007. For details, go to www.who.int/classifications/en/.

Location I consider the location of the household, and whether the child lives in a rural or urban location as an environmental exogenous input. Rural and urban places may differ in access to stores, population density, access to health care institutions, schools, among many other things.

The Cebu-Study-Team (1992) found that the Cebu urban areas are prone to water contamination or to feces exposure, due to population density. However in rural places during heavy downpours, rainwater finds its way into the sewer networks and the springs. Contamination of water contributes to the spread of human diseases.

Growth spurt In the female adolescent production function, I include a dummy variable if the age at menarche is lower than the age of height measurement. In the male adolescent production function, I include one dummy if the age of pubic hair development is lower than the age of height measurement. In the adolescent height production function, I include all the inputs from birth.

Household income and mother's education Household income is a categorical variable with 6 categories. The categories correspond to the percentiles of the distribution of annual household income. The first category corresponds to an income below the 10th percentile, the second between the 10th and 25th percentile, the third between the 25th and 50th percentile, the fourth between the 50th and 75th percentile, the fifth between the 75th and 90th percentile and the last to an income above the 90th percentile.

The mother's education is a categorical variable with 5 categories according to the number of years of schooling. The first category 0 corresponds to 0 years of education, category 1 corresponds to 1-7 years of education, category 2 corresponds to 8-11 years of education, category 3 corresponds to 12-16 years and category 4 corresponds to a number of years of schooling greater than 17.

#### 3.2.3 Age

For infants, age is in months; for older children it is in years. In the different specifications of the model I also include age squared.

Since I am interested in the effects of the inputs at different ages of the child and at different distances between the application of the inputs and the height measurement, I create an age dummy for each range of ages. The fourth column of Table 2 reports the mean ages that correspond to the range of ages I considered.<sup>13</sup>

 $13I$  do observe people at mean age 22 years, but I do not include them in the working sample, because most of them have already completed their height growth.

## 3.3 Inputs from conception to birth

Many researchers suggest that growth in utero may play an important role in determining health in adult life (Barker, 1998). Living in a poor country cannot be underestimated because of the possible malnutrition of the mother. Undernourishment is due to a low supply of nutrients or to a high demand of a fetus that is growing very fast. This can lead to permanent changes in the metabolism, morphology and physiology of the embryo, and consequently of the infant and of the adult (Barker, 1998). The supply of nutrients to the fetus depends on the nutrient store of the mother, on what she eats during pregnancy, on her body size and composition, and on the transmission of nutrients through the placenta (Scott and Duncan, 2002). Furthermore, it is well known that particular vitamins and minerals, such as vitamin A, E, and iron, e.g., play an important role in fetal development.

It would be ideal to have all of this information and to try to understand what is really happening between mother and fetus from conception to birth by computing the nutrient intake of the mother. Because of the complexity of the problem and a lack of data, I use the following variables.

Birth weight I include in the production function the infant's birth weight measured in grams one hour after birth. The quality of the pregnancy relates to the baby's length at birth and, his birth weight (a strong predictor of adult height).

Birth weight is a trait that seems to be inherited probably through the characteristics of the maternal utero. This is the case of normal birth weight. A baby has low birth weight or is small for gestational age when his mass at birth is below a defined limit at any gestational age. The are many reasons for giving birth to a low-birth-weight infant: mother's malnutrition before and during pregnancy, smoking behavior of the mother during pregnancy, the alcohol consumption during gestation, or some maternal diseases (e.g., German measles). Low-birth-weight infants have a higher risk of dying from infectious diseases, or higher risk of developing serious illnesses in later life.<sup>14</sup> The importance of the birth weight is well known and there is a huge literature about it in medicine and economics (e.g., Rosenzweig and Schultz (1983); Behrman and Rosenzweig (2004)).

**Pregnancy's length** The problems of prematurity are very similar to those of low birth weight. A premature birth has a significant impact on the baby's ability to metabolize nutrients. Most pre-term infants with regular weight for their age catch up perfectly, given the right environmental conditions (Tanner, 1990). A

 $14$ Moreover, women who are small at birth have double the risk of having, in turn, babies of low birth weight, which implies intergenerational effects.

baby who is both pre-term and small for his length of gestation may later have deficits in size and ability.

The normal length of gestation is from 37 to 42 weeks. I computed the duration of the gestation as the difference between the last menstrual period and the date of birth. I include a categorical variable indicating whether the child had normal weight and normal term, low birth weight for his gestational age or simply pre-term but with normal weight for his gestational age.

Birth order Birth order has also been found to be a significant and independent predictor of adult height (Steckel, 1995). First-borns children are, during childhood, taller than children born later, since have had a period in which they were alone. More mouths to feed and more ease in contracting infections due to the presence of siblings reduce the growth velocity of the child (Tanner, 1990). I therefore include birth order as an exogenous input.

# 4 Theoretical model and empirical specifications

In this section I present a model for the height production function. This model is strictly related to the papers of Todd and Wolpin (2003, 2007). They estimate a model by considering different specifications of a skill production function for children. I modify their specifications by adapting them to the height formation study and to my data limitations. The similarity of the two studies is that the processes of both height formation and achievement are cumulative processes that depend on the history of inputs chosen by the families, are due to the environment or are simply inherited genetically.

I develop a height production function, since I am interested in technological parameters such as the effect of an exogenous change in one input, keeping all others constant. The technology that links inputs and output is fixed. It is created by nature and cannot be controlled. Economic agents play a negligible role in choosing some of the inputs. The inputs they can choose are nutrition and diseases in the sense of prevention of diseases. They cannot choose either the age or the timing of children's growth.

It is widely known that height depends on the current age and on past inputs, such as health care practices, nutrient intake, disease incidence, environmental elements and genetic factors. A person's height is therefore a cumulative indicator because growth is a cumulative process by which past inputs and genetic endowment are combined in order to obtain height.<sup>15</sup>

 $15 \text{Cuff}$  (2004) writes that "adult stature is a cumulative indicator of net nutritional status over the growth years, and thus reflects command over food and access to healthful surroundings."

Let me define the height production function that relates the height measured at age t to all previous investments in the child. Suppose that for  $t = 0, \ldots, T$  and  $i = 1, \ldots, N$  I have:

- $H_{it}$  the observed height for child i at age t,
- $f(t)$  an age trend,
- $\mathcal{X}_{i,t-1}=(X_{it-1}, X_{it-2}, \ldots, X_{i1}, X_{i0})$  the vector of the observed inputs for child i from birth to age  $t-1$ ,
- $V_{i,t-1}=(V_{it-1}, V_{it-2}, \ldots, V_{i1}, V_{i0})$  the vector of the unobserved inputs for child i from birth to age  $t-1$ ,
- $\mu_i$  the child's biological endowment,
- $\epsilon_{it}$  the measurement error for child i at age t.

Then the **height production function** is given by:

$$
H_{it} = h_t[f(t), \mathcal{X}_{i,t-1}, \mathcal{V}_{i,t-1}, \mu_i, \epsilon_{it}]
$$

The age trend is necessary because the child's age at each wave is different, and if I consider two height measurements for the same individual, their difference also depends on the ages.<sup>16</sup>

The inputs  $\mathcal{X}_{i,t-1}$  are nutrition and diseases. They enter the production function with a lag because I assume that the body needs time to absorb them. Thus I also assume that contemporaneous inputs are not appropriate for this study. I am assuming, for example, that the caloric intake of today does not affect height today, but height depends on past consumption of calories. This temporal lag depends on the structure of the data, in particular, on the distance between waves.

The child's biological endowment is determined at birth and it is constant over time.<sup>17</sup> Finally, the measurement error  $\epsilon_{it}$  is included because there can be errors in the height measurement, even when made by specialists, or measurement errors in the inputs.

To study empirically the height production function, I assume that it is linear in the inputs and in the unobserved endowment, and that the effects of the inputs

<sup>&</sup>lt;sup>16</sup>I use a linear and a quadratic term. I also tried a cubic splines term but there were not huge differences.

<sup>&</sup>lt;sup>17</sup>Case and Paxson (2008b) hypothesize an endowment that changes according to the child's age. But their time-invariant individual effect also includes the environmental factors that in my study are observed and considered as further regressors in the model. Furthermore, I suppose that the gene-environment interactions are the same for each age of the child.

depend both on the child's age and on the distance between the application of inputs and the height measurement. This gives the following model:

$$
H_{it} = f(t) + X_{it-1}\beta_{t,t-1} + X_{it-2}\beta_{t,t-2} + \cdots + X_{i1}\beta_{t,1} + X_{i0}\beta_{t,0} +
$$
  
+
$$
V_{it-1}\rho_{t,t-1} + V_{it-2}\rho_{t,t-2} + \cdots + V_{i1}\rho_{t,1} + V_{i0}\rho_{t,0} +
$$
  
+
$$
\mu_i + \epsilon_{it},
$$
 (1)

and for simplicity I define:

$$
e_{it} = V_{it-1}\rho_{t,t-1} + V_{it-2}\rho_{t,t-2} + \cdots + V_{i1}\rho_{t,1} + V_{i0}\rho_{t,0} + \epsilon_{it}.
$$

The time-varying coefficient  $\beta_{t,x}$  depends on the age t of the child and the distance  $x$  between the time the inputs were applied and the time of the height measurement. Consider for example the child's height at age  $t = 8$ . The effect of the diseases when the child is 5 years old may be different from the effect when the child is 2 years old. This is due to the different distances  $x (\beta_{8.5} \neq \beta_{8.2})$ . The effect of the diseases when the child is 5 years old on height at age 8 may be different than the effects on height at age 6. This is instead due to the different time of the height measures  $(\beta_{8.5} \neq \beta_{6.5}).$ 

Due to the structure of the data and the different growth patterns for boys and girls,<sup>18</sup> and for infants and older children, I estimate the production function for different subsamples. I analyze boys and girls separately and I also splitup "infants" and "adolescents." "Infants" are children between birth and age 2 years, while "adolescents" are people observed between ages 8 and 20 years approximately.<sup>19</sup>

The curse of dimensionality is an important issue in this model. Suppose that I had information at each point in time. In that case the number of parameters to estimate would be equal to  $T * (T - 1)/2$  (pooling all the observations). If I use all the waves available (18) the number of  $\beta$ 's become (18  $\ast$  17)/2 = 153 plus the parameters of additional variables (ex: age, age at menarche, etc.). Table 1 shows the general structure of the  $\beta$ 's parameters. In the empirical application I consider each child's age and I estimate as many production functions as the child's ages considered.

<sup>&</sup>lt;sup>18</sup>At birth the typical boy grows faster than the typical girl, but the velocities become equal around 7 months and then girls grow faster until age 4. There are no differences until they reach adolescence. The typical girl is slightly shorter than the typical boy at all ages until adolescence. She is taller during her adolescence spurt because it takes place two years before the male spurt (Tanner, 1990).

<sup>&</sup>lt;sup>19</sup>The labels are not technically correct since an infant is between 1 month and 12 months old, while an adolescent is usually between 13 and 19 years old.

#### 4.1 Different specifications

Behrman and Deolalikar (1988) summarize the most common estimation problems in health and nutrition studies in developing countries, and I report the most relevant for this study. The first problem is endogeneity; e.g., the inputs and the outcome are determined simultaneously. The second problem regards the omitted variables. The exclusion of important variables can give biased estimates. A third problem is sample selectivity. This arises when the people in the sample are selected. For example, the weakest children die and thus only the strongest individuals stay in the sample. A fourth problem is the errors-in-variables problem. The variables I use are not self-reported and therefore this problem is not a big issue in my analysis. A fifth problem is the appropriate lag structure for the variables included in the model. Using only current data may not be sufficient when the effect of past variables are relevant. The CLHNS data contain detailed information on past inputs, and including them makes a considerable contribution to the existing health production functions.

In order to estimate (1), I consider two different specifications based on two estimation methods. They rely on different assumptions aimed at solving the open issues listed above.

Cebu-Study-Team (1992) and Liu, Mroz, and Adair (2009) use another specification that includes lagged values of the outcome and contemporaneous inputs in the model instead of the historical inputs. In the cognitive skills literature this specification is called "value added" specification. When data on past inputs are missing, the use of lagged outcome is quite common. However, the lagged outcome is correlated with the measurement error by construction, and additional lagged outcome measures can be used as instruments. Since past inputs are available, and I am specifically interested in their impact on height, I do not consider this specification. A lagged measure of height would capture almost all of the variability and it would not allow me to distinguish between the effects of nutrition and non-nutrition inputs.

#### 4.1.1 Naive specification

My first specification imposes the following set of assumptions:

(a) Included inputs are not correlated with endowment

$$
E[\mu_i|X_{it-1}, X_{it-2}, \ldots, X_{i0}] = 0.
$$

(b) Measurement error is orthogonal to the included inputs (strict exogeneity assumption) conditionally on  $\mu_i$ 

$$
E[\epsilon_{it}|X_{it-1}, X_{it-2}, \ldots, X_{i0}, \mu_i] = 0.
$$

(c) Omitted inputs are orthogonal to the included inputs

$$
E[V_{it-1}, V_{it-2}, \dots, V_{i0} | X_{it-1}, X_{it-2}, \dots, X_{i0}] = 0.
$$

These assumptions allow me to estimate the  $\beta$ 's by OLS. This specification is called naive because it imposes very strong restrictions on the production function (1).

Let me analyze these assumptions one at a time:

Assumption (a) fails if the choice of inputs is correlated with the endowment.

Assumption (b) fails in the case of endogenous inputs. If you think that parents (or the child when he is old enough) choose the inputs to improve health outcomes according to a dynamic or sequential process, then the exogeneity of the measurement error fails. The reason is that these choices are likely to be based on past outcomes or past shocks.

Assumption (c) fails if there are omitted variables that are correlated with the observed inputs. Suppose, for example, that the protein intake is unobserved. Protein intake is likely to be correlated with caloric intake, which is an observed input. To account for the omitted variables bias I estimate a hybrid production function that includes in the naive specification annual household income and mother's education.<sup>20</sup> The hybrid health production functions are production functions that contain some of the health inputs and the determinants of the other non-available inputs.<sup>21</sup>

#### 4.1.2 Within-child fixed effects specification

This specification is feasible because the children are observed more than once, and it is possible to rely on several outcome and input measurements.<sup>22</sup> Consider the technology (1) at two different ages, t and s, with  $t > s$ :

$$
H_{it} = f(t) + X_{it-1}\beta_{t,t-1} + X_{it-2}\beta_{t,t-2} + \cdots + X_{is+1}\beta_{t,s+1}
$$
  
+
$$
X_{is}\beta_{t,s} + X_{is-1}\beta_{t,s-1} + \cdots + X_{i1}\beta_{t,1} + X_{i0}\beta_{t,0} + \mu_i + e_{it}
$$
  

$$
H_{is} = f(s) + X_{is-1}\beta_{s,s-1} + X_{is-2}\beta_{s,s-2} + \cdots + X_{i1}\beta_{s,1} + X_{i0}\beta_{s,0} + \mu_i + e_{is}
$$

 $20$ To solve the omitted variables bias it would also be possible to express the missing inputs as functions of current and past family income, prices and preference shocks. Once those omitted input demand equations are specified they can substitute the missing inputs in the production function (Todd and Wolpin, 2007).

<sup>&</sup>lt;sup>21</sup> Once controlled for income and mother's education the hybrid effect of the inputs on height is generally a biased estimate of the true technical relationship (other inputs held constant) embodied in the health production function (Rosenzweig and Schultz, 1983).

 $^{22}$ A within family specification would be interesting, but the data contain anthropometric measurements of some siblings but not all the information about siblings' net nutrition.

Grouping the inputs applied at the same age and differentiating gives:

$$
H_{it} - H_{is} = f(t) - f(s) + X_{it-1}\beta_{t,t-1} + X_{it-2}\beta_{t,t-2} + \cdots + X_{is+1}\beta_{t,s+1} + X_{is}\beta_{t,s} + X_{is-1}(\beta_{t,s-1} - \beta_{s,s-1}) + \cdots + X_{i1}(\beta_{t,1} - \beta_{s,1}) + X_{i0}(\beta_{t,0} - \beta_{s,0}) + e_{it} - e_{is}
$$
\n(2)

The parameters resulting from equation (2) are the specific age input effects for the inputs applied between the two ages and the difference in the parameters for the inputs applied before the younger height  $H_{is}$ .

Consider the following example. Suppose that I consider a child's height at 2 and 3 years and I group inputs applied at the same age. Suppose the information is collected once a year. The difference in height between the two ages becomes:

$$
H_{i3} - H_{i2} = f(3) - f(2) + X_{i2}\beta_{3,2} + X_{i1}(\beta_{3,1} - \beta_{2,1}) + X_{i0}(\beta_{3,0} - \beta_{2,0}) + e_{i3} - e_{i2}
$$

The parameters in this equation are the specific age input effect  $\beta_{3,2}$  for the inputs applied at age 2 and the difference in the parameters  $\beta_{3,1} - \beta_{2,1}$  and  $\beta_{3,0} - \beta_{2,0}$  for the inputs applied at ages 1 and 0, respectively.

The coefficients associated with the inputs applied before the younger height cannot be identified.<sup>23</sup> In the empirical application I always consider the first age  $s = 0$  and therefore  $H_{is} = H_{i0}$  is the height at birth. Doing so, I can identify all the parameters of the inputs applied between the two ages and I can compare them with the parameters estimated using the naive specification.

This second specification imposes the following set of assumptions:

- (a) Included inputs are not correlated with the endowment: not need be assumed.
- (b) Measurement error is orthogonal to the differenced included inputs (strict exogeneity assumption) conditionally on  $\mu_i$ .
- (c) Differenced omitted inputs are orthogonal to the differenced included inputs.
- (d) Later input choices are invariant to prior own height.<sup>24</sup>

$$
E[H_{it}|X_{i0},\ldots,X_{it-1},X_{it},X_{it+1},\ldots,X_{iT}] = X_{it-1}\beta_{t,t-1} + \cdots + X_{i0}\beta_{t,0}.
$$

These assumptions allow me to estimate the  $\beta$ 's by fixed effects (FE). I explain them as follow:

<sup>&</sup>lt;sup>23</sup>This includes also the inputs applied from conception to birth for which I use proxies, for example, birth weight. Birth weight is a time-invariant variable, and it is not identified from the within-child estimator.

<sup>&</sup>lt;sup>24</sup>In the case of the presence of contemporaneous inputs  $X_{it}$ , this assumption would require the orthogonality condition between  $e_{is}$  and  $X_{it}$ .

Assumption (a) need not be assumed because the within-child fixed effect estimator eliminates the endowment from equation (2). This estimator deals with the endowment heterogeneity.

Assumptions (b) and (d) deal with the potential endogeneity of the inputs. The endogeneity can be due to feedback effects. Suppose, for example, that a child is very small. It is plausible that the parents will give him more food to help his growth. Using an instrumental variables approac, h it could be possible to estimate the input demand equations for the endogenous inputs. I tried to use different sets of instruments as robustness checks.

Assumption (c) means that omitted inputs are constant over time and by the fixed effect estimators they are eliminated. To account for the omitted variables bias, I also estimate a hybrid production function through the fixed effects specification using annual family income and mother's education as proxies.

# 5 Empirical results

### 5.1 Estimates of infant height production function

To estimate the infant production function I use only four monthly spaced waves, starting from birth using information at the mean ages 0, 4, 8, 12, 16, 20 and 24 months. This reduces the number of parameters to include in the specification and enlarges the temporal window between two measurements from 2 months to 4 months.

The empirical model for the infants includes inputs from conception to birth and from birth to the age before the age when height is measured. Net nutrition for the infants consists of diseases, caloric intake, breast milk and breast milk times caloric intake. They all have the same lagged structure. I include the interaction term because the caloric intake of the infants excludes the caloric intake of breast milk. Table 4 presents the parameters of the production function for the caloric intake with the relative age of the child and the age at which inputs are applied. The number of parameters depends both on the distance between the outcome and the input, and on the child's age. The calorie intake, breast feeding and disease inputs enter the model multiplied by the child's age dummies.

The other covariates are mother's height, location, birth weight, length of the pregnancy and birth order. They are time-invariant variables, constant for the entire life of the child, except location, which is a contemporaneous time-varying input. None of them are interacted with the child's age.

In the naive specification I estimate the infant height production function separately foreach age of the child.<sup>25</sup> Doing so, is like working with a cross-section

 $^{25}I$  do not pool all of the observations due to the large number of parameters that need to be

data because I observe the infant in a specific range of ages only once. This allows me to get specific parameters that account both for the infant's age and for the distance between height measurement and application of the inputs.

I then use the within-child fixed effects specification. To get the 18 parameters reported in Table 4 using the within-child fixed effects specification, I estimate the fixed effect estimator on a couple of ages, where one of the two is always the height at birth. Hence I am able to identify the effects of inputs at specific ages for each age of the infant and I can compare them with the naive estimates. $26$ 

Tables 6 and 7 show the results of the naive and fixed effects specifications separately for boys and girls. I report the production functions only for infants who are 12 and 24 months old.<sup>27</sup> In general there is not a big difference between the naive and fixed effect estimates.

The inputs from conception to birth are time-constant variables and therefore are dropped in the fixed effects specification. The naive specification shows that birth weight and birth order are always significant for each age and sex of the infant. An increase of 100g in birth weight produces an increase in the infant's height of about 0.2 cm at all ages, with slight variations between boys and girls. The older the infant, the bigger the negative impact of the parity. If a boy is 12 months old, having one older sibling reduces his height by 0.26 (0.23 in the hybrid production function) and by 0.34 (0.32 in the hybrid production function) if he is 24 months old. In girls the effect is smaller. The fact of being premature or premature and small-for-dates with respect to a normal baby does not appear to affect infant's height, probably because the birthweigh captures almost the entire effect.

The mother's height is always positive and significant. An increase of 1 cm in mother's height produces an increase in the infant's height of about 0.18 cm if the infant is a 24-month-old boy and of about 0.16 cm if the infant is a girl. The younger the infant, the lower the effect of mother's height.

estimated.

 $H_{24} - H_0 = \alpha^{24} + X_{i20}\beta_{24,20} + X_{i16}\beta_{24,16} + \cdots + X_{i4}\beta_{24,4} + X_{i0}\beta_{24,0}$  $H_{20} - H_0 = \alpha^{20} + X_{i16}\beta_{20,16} + \cdots + X_{i4}\beta_{20,4} + X_{i0}\beta_{20,0}$  $H_{16} - H_0 = \alpha^{16} + X_{i12}\beta_{16,12} + \cdots + X_{i4}\beta_{16,4} + X_{i0}\beta_{16,0}$  $H_{12} - H_0 = \alpha^{12} + X_{i8}\beta_{12,8} + \cdots + X_{i4}\beta_{12,4} + X_{i0}\beta_{12,0}$  $H_8 - H_0 = \alpha^8 + X_{i4}\beta_{8,4} + X_{i0}\beta_{8,0}$  $H_4 - H_0 = \alpha^4 + X_{i0} \beta_{4,0}$ 

<sup>27</sup>The height production function estimates for infants 4, 8, 16 and 20 months old are available upon request.

<sup>&</sup>lt;sup>26</sup>I run the following regressions where I report only the inputs time-varying (in  $\alpha$ <sup>\*</sup> there are trends and time-varying variables that enter only at the current time e.g.location):

Living in an urban area instead of in a rural one does not seem to have a significant impact on the infant's height. Nutrition has a positive and significant effect on height if applied at a short distance from the time of height measurement. The older the infant, the bigger the effect of the nutrition inputs. Nutrition inputs do not have a relevant effect on girls' height when they are 12 months old (or younger). If a 12-month-old boy was breast-fed in the previous months, that increases their height by 0.8 cm (Table 6). Between 12 and 24 months, caloric intake and breast milk have positive effects on both boys' and girls' growth. Consider a 24-month-old boy and that the nutrition inputs are applied at age 20 months and the non-hybrid production function is used (Table 7). If the caloric intake increases by 100 kcal and the boy is not breast-fed, then height increases by 0.09 cm (0.1 cm in the fixed effects specification); if he is also breastfed height increases by  $0.095cm+1.576cm-0.17cm=1.5$  cm  $(0.9 \text{ cm in the fixed effects specification})$ .

Diseases always have a significant and negative impact on boys' height when the diseases occur at early ages: at birth or when the infant is 4 months old. Experiencing at least one disease<sup>28</sup> decreases height by  $0.6-2.3$  cm, depending on the specification, infant's age and sex. The older the boy, the more he is affected by sicknesses. The younger the girl, the more she is affected by sicknesses.

## 5.2 Estimates of adolescent height production function

In the data used to estimate the adolescent height production function, the waves are no longer approximately equally spaced. There are intervals of about 3-4 years and a jump of 6 years between infancy and middle childhood that starts approximately at the age of 8. Table 2 reports in light blue the ranges of ages considered. The oldest people are adolescents, mean age 18.7 years. Most of them have completed their growth and therefore their height production function gives the complete picture of what determines their height from birth to early adulthood.

The variables entering the production function are inputs from conception to birth, net nutrition, location and mother's height. Table 5 reports the parameters estimated for caloric intake. According to the time when the input was applied, the variables included with the lagged structure are caloric intake for nutrients different from breast milk, breast milk, their interaction term, total caloric intake, infants' diseases and adolescents' diseases. Those variables are multiplied by the age dummies to account for the different child's age and distance between height measurement and application of the input.

As for the infants height production function, in order to apply the within-child fixed effects estimator I pair ages, with one always the height at birth.

Tables 8, 9, 10 and 11 report the results separately for boys and girls, specifi-

 $^{28}$ At least one of the diseases listed in the previous section.

cations and type of production functions (hybrid or not hybrid). They represent the height production functions for people mean age  $t = (8.5, 11.5, 15.5, 18.7)$ . The inputs considered are all of the past inputs from birth to the previous height measurement age.

The inputs from conception to birth are still significant. An increase in birth weight of 100g produces an increase of about 0.25-0.3cm in height, with small variations between boys and girls. This is true for all adolescents analyzed. A unit increase of the birth order reduces the adolescent's height by about 0.2-0.3cm, according to age and sex of the person. Being pure pre-term has a positive effect on height in boys 11.5 and 15.5 years old, which is unexpected, but it is probably due to a strong catch-up.<sup>29</sup> Mother's height is always positive and significant with bigger coefficients than in the infant production function. The older the child, the stronger the relation between his height and his mother's height. Being sexually mature is extremely relevant if the girl is 8.5 years old, with an increase in height of about 2.4-8.5cm depending on the specification and on the type of production function. If the girl is 11.5 years and she has already reached menarche, her height increases by 7-8 cm.<sup>30</sup>

Concerning the environmental variables and using the naive specification, I find that living in an urban area has a negative and significant impact (-0.8 cm) on girls age 15.5. Living in a city may increase the likelihood of spreading diseases.

Nutrition appears to be positive and significant in boys and girls when applied at short distance to the height measurement.<sup>31</sup> Nutrition assumed in infancy has an effect on children only until age 8.5, but not after they become teenagers. Nutrition has a higher impact when adolescents are  $11.5$  or  $15.5$  years old. Increasing caloric intake by 100g increases height by 0.1-0.2cm according to the type of production function, sex and specification. In the fixed effect specification the parameters are slightly bigger than in the naive specification. This period coincides with the adolescence spurt and that could explain the greater importance of nutrients.

Diseases experienced in early life negatively affect boys' and girls' height  $(-3)$ or -5cm) when they are 8.5 or 11.5 years old. For girls, the reduction in height due to diseases is bigger when the fixed effect specification is used, while for boys the reduction is higher in the naive specification. During later adolescence (ages 15.5 and 18.7) the disease inputs applied at any age are not relevant for girls. The boys are, instead, negatively affected by chronic illnesses occurred at age 8.5. Those diseases of long duration may have started years before (mostly during

<sup>&</sup>lt;sup>29</sup>Eckhardt et al. (2005) and Adair (1999) found that Filipino children exhibit catch-up growth after age 2.

 $30$ In poor countries the age at menarche is often later than it is in rich countries, because malnutrition retards growth.

<sup>&</sup>lt;sup>31</sup>Sometimes breast milk has a negative effect and that is not an expected result but it depends on the age of the infant and thus it can be only a temporary effect.

early childhood, between ages 2 and 8). The reduction in height caused by those diseases is about -2.5cm in the naive specification and -3.5cm in the fixed effects specification.

## 6 Robustness

## 6.1 Potential endogeneity of observed inputs

Two papers analyze the endogeneity issues when estimating infants' health production function using the Cebu data. The first paper is by the Cebu-Study-Team (1992) and they analyze four different outcomes: gestational age, weight, diarrhea and respiratory infection. They focus only on the first year of life. They use a "value-added" specification, where each outcome is regressed on the previous outcome measure and on contemporaneous inputs. Thus, all the past inputs collapse in the past outcome measure. An instrumental variables approach is used to find the effects of the contemporaneous endogenous inputs. Since I, instead, consider all the past inputs I should find instruments for all of them. Among their endogenous inputs there are also birth weight, gestational age, diarrhea, weight, febrile respiratory infection, different breast-feeding patterns, preventive health care for infants and personal hygiene.

The second paper is by Liu, Mroz, and Adair (2009), who look at children in the first two years of life. They estimate an empirical model that includes parents' demand equations and the child's health production functions. Their analysis is based on a dynamic model of parental investments. They jointly estimate four health outcomes: weight, height, incidence of diarrhea and incidence of severe respiratory infections. They use, as in the Cebu-Study-Team (1992), a "valueadded" specification of the health production function. The endogenous inputs are breast-feeding choices, caloric intake for supplement food, prenatal care, mother's working and preventive health care. The authors find evidence of compensatory parental behavior, but they argue that it was impossible to observe all aspects of parents' behavior. Hence, it was impossible to disentangle the effects of the observable behavioral responses from the effects of the unobservable behavioral responses due to the choices of missing health inputs. Furthermore, they consider diarrhea and respiratory infections as health outcomes, but they do not consider them as inputs in the height production function. Since I consider only height as an outcome and diseases as relevant inputs, my model is not directly comparable with Liu, Mroz, and Adair's (2009) model.

To address the endogeneity issue, I also apply an instrumental variables approach. The inputs that are potentially endogenous are caloric intakes, breast

feeding and diseases.<sup>32</sup> In this paper the endogeneity may be caused by feed back effects.<sup>33</sup> The parents may change their behavior depending on their child's health status. If, for example, the child is malnourished, his parents may increase his nutrient intake, or if the child is sick, his parents may improve the preventive health care. To estimate the input demand equations, I consider two sets of instrumental variables: one for the behavioral inputs of the infants' height production function and one for the behavioral inputs of the adolescents' height production function. The instrumental variables are reported in the Appendix in Tables 13 and 14.<sup>34</sup> Some of them are the same as in the empirical work by Cebu-Study-Team (1992). These instrumental variables can affect the parents' choices in terms of food consumption and health care, but at the same time they are not correlated with the child's (adolescent's) height. I need at least one instrument per each lagged input. I use lagged values of the instrumental variables to have instruments and inputs measured at the same point in time.

Unfortunately, the instruments are weak, especially for the diseases inputs. Table 15 and the tests following the table show, as an example, the weakness of the instruments used in the height production function of an infant 24 months old estimated through the naive non-hybrid specification.<sup>35</sup> There can be several reasons for that: the lack of inclusion of some important prices, the common food home production that may be less influenced by the market's prices, the high correlation between instruments close in time, or the fact that individuals of the same family may be affected differently by changes in prices or village characteristics, just to mention a few. Consider, for example, the price of rice in January 1983. It is likely to be very similar to the price in May 1983. Or suppose, for example, that the prices of powdered milk increases, then parents may reduce their consumption of other goods to provide the same amount of milk for their infant.

Furthermore, I am aware of the potential endogeneity of net-nutritional inputs, but if missing inputs depend on investments in children, they are likely to be correlated with both the instruments and the observed inputs (Todd and Wolpin, 2003). It is also important to note that if the omitted inputs are correlated with the included inputs, then the IV procedure is not valid.

<sup>32</sup>One can also argue that birth weight, birth order and gestational age are endogenous. If the mother has older sons, she can change her behavior during the pregnancy according to the past experience (Rosenzweig and Wolpin, 1995).

<sup>&</sup>lt;sup>33</sup>Endogeneity due to simultaneity is not an issue here, because the model does not include contemporaneous inputs.

<sup>34</sup>I thank the National Statistics Office of the Philippines, which provided me with the CPI and inflation rates used to deflate prices.

<sup>&</sup>lt;sup>35</sup>Almost all the production functions estimated (according to the different ages of the child and the specifications,) with the IV approach present bad instruments, even when I consider different sets of instruments for each lagged input.

#### 6.2 Omitted variables bias

I test the possibility of omitted variables bias by looking at the coefficients of household income and mother's education in the hybrid production functions. If they are significantly different from zero, then they need to be included in the functions. Family income is positive and significant in girls of mean age 8.5 years, while a better socio-economic situation of the family, with both higher income and higher mother's education, is positive and significant for boys when they are on average 11.5 years old. That means that omitted inputs seem to affect height when children begin their growth spurt.

#### 6.3 Sample selection bias due to attrition

The last wave considered in the empirical exercise contains 2023 people (1071 males, 952 females). Between the baseline and the last wave around 35% of the children are lost, and 18% before the age of 2. This high attrition is common in long-term longitudinal studies and in data that come from developing countries.<sup>36</sup> The highest attrition rate is between wave 12 and 13, that is, between infancy and mean age 8.5. From wave 12 conducted in 1985-86 and wave 13 conducted in 1991-92 there are approximately 6-7 years of missing information, the children's childhood.

The two main reasons for attrition are death and migration. Two hundred and twenty-five (7.3% of the sample) children die: 167 (5.4%) in the first 2 years of life, 44 between the ages of 2 and 8, 14 children die during adolescence. In total 129 boys and 96 girls die.

The remaining 28% are mainly lost because of migration. The Cebu-Study-Team (1992) tested for selectivity of infants and the results show that the omitted variables that influence migration decisions do not greatly overlap with those that determine child health. I tested for selection on unobservables of adolescents who migrate and the conclusions are the same. Therefore I consider that attrition due to migration can be disregarded.

Eckhardt et al. (2005) used the same longitudinal survey to study the compensatory growth that occurred after 2 years of age among the children who were stunted in infancy. They report that people who died tended to be of very low socio-economic status and grew up poorly until their deaths, while those who moved tended to be of higher socio-economic status and from urban areas. In their study, attrition does not represent a problem.<sup>37</sup> Unfortunately, there is no

<sup>36</sup>Alderman et al. (2001) study attrition in three different longitudinal data sets from developing countries. Even if attrition is very high, it is not a general problem for obtaining consistent estimates.

<sup>&</sup>lt;sup>37</sup>The reason being that only a small proportion of children in the poorest health conditions

information about the interviewers or other exclusion restrictions that could be used to test and correct the selection on unobservables that determine death. Hence, given the rather low percentage of children who died, I keep them in the sample.

## 6.4 Model specification

The naive and fixed effect specifications give similar results. That is true for the coefficients and for the predictions, as can be seen in Figure 1. The big difference about the naive and within-child fixed effect specifications is assumption (a) about the endowment. The fixed effects allow the inputs to be endogenous with respect to the endowment. It is plausible that investments in children are correlated with the unobserved endowment. To select between the two specifications I look at the out-of-sample goodness of fit.

I use the cross validation procedure to test the goodness of fit out of sample. This procedure can be used to compare non-nested models and, under some statistical assumptions, the root mean square error (RMSE) is used to summarize the errors. I do the cross validation using random holdout samples. I randomly divide the sample in 8 subsamples of equal size. I estimate the model on 7 of the 8 subsamples and I compute the RMSE for the left-out subsample. I repeat that, considering each time a different holdout subsample. I then sum the RMSE obtaining the total RMSE for that model. I repeat the subsetting 5 times and I compute the average total RMSE.

Table 12 shows the RMSE of the different specifications per each age of the person. The model with the smallest RMSE performs best with a data set that is independent of the data used to train the model. The naive non-hybrid specification reports the lowest RMSE for infants and for the oldest adolescents. When the child is between 1 and 11.5 years old, the naive hybrid specification has the smallest RMSE, for both boys and girls. In no case do the fixed effects perform better.

# 7 Conclusions

In this paper I study the determinants of height formation, building a height production function. I consider the cumulative nature of physical development, taking into account both the age of the child and the distance between application of the inputs and height measurement. I carefully consider the biological inputs from conception to early adulthood and I also estimate a hybrid production function that accounts for the missing inputs.

were lost.

The results show a systematic effect of net nutrition on the child's height, looking at different ages of the child. The older the child, the smaller the nutrition effects and the stronger the disease effects. I found that in most of the cases nutrition has an impact at a short distance, while diseases affect height if applied at early ages or at a long distance from the height measurement. Boys' height is negatively influenced by diseases, and that is true at any age. Girls, instead, present two critical stages. Diseases experienced during infancy matter in a girl's height when she is younger than 1 year and during her growth spurt, when she is between 8 and 11 years old. The effects of diseases are much bigger than the effects of nutrition. Diseases experienced in early life really matter for good growth, especially for boys.

The model, indeed, shows the importance of including past inputs and of studying their effects according to different ages and sex of the children. Growth in utero, infancy and the pre-puberty years turn out to be critical stages in the process of height formation.

I use cross-validation to select between the naive and fixed effects specifications. I based the cross-validation on the RMSE criteria. The naive specification holds the smallest RMSE per each age of the child, and therefore, it predicts better out-of-sample than the fixed effects specification. However, the naive specification is based on a strong assumption that requires the endowment to not be correlated with the observed inputs. And one may argue that the cross-validation is based on level predictions. It would be interesting in the future to study growth in height and see which is the specification that performs better.

In any case, the results of this paper can be important for policy makers to know what factors determine a person's height at different stages of her life in a poor country, which periods are critical, and which inputs have the strongest impact on growth.

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# 8 Tables and Graphs



## Table 1: Lagged Inputs Parameters -  $\beta$ 's

Number of  $\beta$ 's parameters to estimate according to the person's age at height measurement.

<b>Surveys</b>	Min age	Max age	Mean age	St. dev.	N
Months					
*Delivery Survey 1983-4	$\overline{0}$	$\Omega$	$\Omega$	$\overline{0}$	3080
Follow-up n.1	1.4	3.4	2.05	.15	2878
*Follow-up n.2	3.4	5.7	4.05	.15	2802
Follow-up n.3	5.4	7.3	6.05	.15	2717
*Follow-up n.4	7.5	9.1	8.04	$.13\,$	2665
Follow-up $n.5$	9.4	11.2	10.07	.15	2625
$*$ Follow-up n.6	11.6	13.1	12.07	.17	2594
Follow-up n.7	13.0	15.0	14.07	.17	2549
*Follow-up n.8	15.5	17.2	16.07	.17	2507
Follow-up n.9	17.7	19.1	18.06	.17	2507
*Follow-up n.10	19.6	21.1	20.06	.18	2498
Follow-up n.11	21.7	23.0	22.04	.16	2460
$*$ Follow-up n.12	23.6	25.2	24.05	.15	2448
Years					
1991-2	7.5	8.7	8.5	.05	2264
1994-5	10.6	13.0	11.5	.40	2182
1998-9	14.1	16.8	15.5	.67	2089
2002	17.9	19.8	18.7	.34	2023
2005	20.7	22.3	21.5	.30	1888

Table 2: Panel structure and ranges of ages

The \* indicates the waves used in the infant production function.

The light blue indicates the waves used in the adolescent production function.



Wave	Mean	Age at	Age at	Age at	Age at	Age at	Age at
	Monthly Age	1 Period	2 Period	3 Period	4 Period	5 Period	6 Period
	at height	$_{\rm Lagged}$	Lagged	Lagged	$L$ agged	Lagged	Lagged
	measure $(t)$	kcal	kcal	kcal	kcal	kcal	$_{\rm kcal}$
$\Omega$	0	$\cdot$ $\cdot$ $\cdot$	$\cdots$	.	.	$\cdots$	$\cdots$
$\overline{2}$	4	0 $(\beta_{4.0})$	$\cdots$	.	.	$\cdots$	$\cdots$
$\overline{4}$	8	$4(\beta_{8,4})$	0 $(\beta_{8.0})$	.	.	$\cdots$	$\cdots$
6	12	$8(\beta_{12.8})$	$4\ (\beta_{12.4})$	0 $(\beta_{12.0})$	$\cdots$	$\cdots$	$\cdots$
8	16	12 $(\beta_{16,12})$	$8(\beta_{16.8})$	$4\ (\beta_{16,4})$	0 $(\beta_{16.0})$	$\cdots$	$\cdots$
10	20	16 $(\beta_{20.16})$	12 $(\beta_{20,12})$	$8(\beta_{20,8})$	$4(\beta_{20.4})$	0 $(\beta_{20.0})$	$\cdots$
12	24	$20 (\beta_{24.20})$	16 $(\beta_{24.16})$	12 $(\beta_{24.12})$	$8(\beta_{24.8})$	$4(\beta_{24.4})$	0 $(\beta_{24.0})$

Table 4: Infants' Height Production Function - Calorie intake and ages

Table 5: Adolescent's Height Production Function - Calorie intake and ages

Wave	Mean	Age at	Age at	Age at	Age at	Age at	Age at	Age at
	Yearly Age	Period	2 Period	3 Period	4 Period	5 Period	6 Period	7 Period
	at height	$_{\rm Lagged}$	$_{\rm Lagged}$	$_{\rm Lagged}$	Lagged	$L$ agged	$_{\rm Lagged}$	Lagged
	measure $(t)$	kcal	kcal	kcal	kcal	kcal	kcal	kcal
13	8.5	$24m (\beta_{8.5.24m})$	$1\ (\beta_{8.5.12m})$	$4m (\beta_{8.5.4m})$	$0\ (\beta_{8.5.0})$	.	$\cdots$	$\cdots$
14	11.5	$8.5\ (\beta_{11.5.8.5})$	$2(\beta_{11.5.24m})$	$12m (\beta_{11.5,12m})$	$4m (\beta_{11.5.4m})$	$0\ (\beta_{11.5.0})$	$\cdots$	$\cdots$
15	15.5	$11.5\ (\beta_{15.5,11.5})$	$8.5~(\beta_{15.5.8.5})$	$24m (\beta_{15.5.24m})$	$12m (\beta_{15.5,12m})$	$4m (\beta_{15.5.4m})$	$0\ (\beta_{15.5.0})$	$\cdots$
16	18.7	$15.5\ (\beta_{18.7,15.5})$	11.5 $(\beta_{18.7,11.5})$	$8.5~(\beta_{18.7.8.5})$	$24m (\beta_{18.7,24m})$	$12m (\beta_{18.7,12m})$	$4m (\beta_{18.7.4m})$	$0\ (\beta_{18.7,0})$



Table 6: Height production function of an infant 12 months old. Table 6: Height production function of an infant 12 months old.

Each model (each column) includes the age in months and the age in months squared.

The letter m in the inputs indicates months (for example, 4m means 4 months). A change of one unity in caloric intake corresponds to 100 kcal. Bach model (each column) includes the age in months and the age in months squared.<br>The letter m in the inputs indicates months (for example, 4m means 4 months). A change of one unity in caloric intake corresponds to 100 k

 The hybrid production function includes annual household income and mother's education. † means that the parameters are 0 or not well estimated because of few cases of spurt. means that the parameters are 0 or not well estimated because of few cases of spurt.



The hybrid production function includes annual household income and mother's education.

Table 7: Height production function of an infant 24 months old. Table 7: Height production function of an infant 24 months old.



Table 8: Height production function of a child 8 years old. Table 8: Height production function of a child 8 years old.

•†

 The hybrid production function includes annual household income and mother's education. means that the parameters are 0 or not well estimated because of few cases of spurt.



Table 9: Height production function of a child 11.5 years old. Table 9: Height production function of a child 11.5 years old.

•†

 The hybrid production function includes annual household income and mother's education. means that the parameters are 0 or not well estimated because of few cases of spurt.



Table 10: Height production function of a child 15.5 years old. Table 10: Height production function of a child 15.5 years old.

The hybrid production function includes annual household income and mother's education.



The letter m in the inputs indicates months (for example, 4m means 4 months). A change of one unity in caloric intake corresponds to 100 kcal.

The letter m in the inputs indicates months (for example, 4m means 4 months). A change of one unity in caloric intake corresponds to 100 kcal.

 $\bullet$  The hybrid production function includes annual household income and mother's education. The hybrid production function includes annual household income and mother's education. † means that the parameters are 0 or not well estimated because almost everybody reached the spurt. means that the parameters are 0 or not well estimated because almost everybody reached the spurt.

Table 11: Height production function of a child 18.7 years old. Table 11: Height production function of a child 18.7 years old.

	<b>Boys</b>				Girls			
	<b>NAIVE</b>		<b>FIXED EFFECTS</b>		<b>NAIVE</b>		<b>FIXED EFFECTS</b>	
Mean Age	Non-Hybrid	$Hvbrid^{\bullet}$	Non-Hybrid	$Hvbrid^{\bullet}$	Non-Hybrid	$Hvbrid^{\bullet}$	Non-Hybrid	$Hvbrid^{\bullet}$
$18.7$ years	73.291†	73.378	75.753	75.254	74.724†	75.086	77.409	77.664
$15.5$ years	50.323†	50.629	56.748	56.501	67.330†	68.330	70.323	69.055
$11.5$ years	53.892	53.564†	57.134	57.196	51.199	51.195†	53.998	54.181
8.5 years	40.523	40.209 <sup>+</sup>	43.155	43.275	40.041	39.304†	43.145	43.051
24 months	25.749	25.593†	28.342	28.596	25.895	25.767†	28.328	28.276
20 months	24.811	24.601†	27.372	27.925	24.966	24.762†	27.361	23.522
16 months	23.084	22.943 <sup>+</sup>	25.855	26.164	23.215	23.144†	25.803	25.897
12 months	34.783	34.671†	36.959	37.183	34.953	34.867†	36.952	36.899
8 months	47.349†	47.360	48.624	49.136	47.451†	47.493	48.520	48.537
4 months	60.508†	60.515	61.100	61.125	60.537†	60.556	61.184	61.176

Table 12: Cross Validation Results

Random holdout sample. A number of 8 subsamples of equal size are created. The model is estimated on 7 of the 8 subsamples and the RMSE is computed. This is repeated, considering each time a different holdout subsample. The total RMSE for that

model is obtained summing all the RMSE. The average total RMSE is obtained replicating this procedure 5 times.

• The hybrid production function includes annual household income and mother's education.

† corresponds to the lower RMSE per age of the person.



Figure 1: Height predictions per each age of the child

# APPENDIX





The temporal window for the infants is 2 years and I suppose that there have been not relevant changes in the household's characteristics measured only in the baseline.<br>There are two community surveys for infants, collecte The temporal window for the infants is 2 years and I suppose that there have been not relevant changes in the household's characteristics measured only in the baseline.

There are two community surveys for infants, collected in 1983 and 1986. For the central years I use the mean of the two measurements per each barangay's variable.

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Table 14: Instrumental variables for teenagers' endogenous inputs. Table 14: Instrumental variables for teenagers' endogenous inputs.

All prices are monthly and deflated. I report the mean prices that correspond to a specific age of the teenager.

All prices are monthly and deflated. I report the mean prices that correspond to a specific age of the teenager.





Included instruments: Age; Age Sq; Birth Order; I-Urban; Birth weight; I-Premature&Small-for-dates; I-Premature; Mother's height

Excluded instruments: Kerosene price at 20m, Cooking oil price at 16m, Evaporated milk price at 12m, Formula price at 8m, Banana price at 4m, Corn price at birth, Powdered milk price at 20m, Cereal price at 16m, Rice price at 12m, Pork price at 8m, Dried fish price at 4m, Egg price at birth, Dirt road at 20m, Elevaton at 16m, Pop density at 8m, % of houses with electricity at 4m, Water sup at birth, Water sup at 20m, Distance road at birth, Refrigerator at birth, Walk cann at birth, Walk formula at birth, Walk inft at birth, Time priv hf at birth, Time pub hf at birth, Time trad hf at birth, Father's age at birth, Med insurance at birth, Religion at birth, Season at 16m, Gravel road at 12m

#### Underidentification tests

Ho: matrix of reduced form coefficients has rank=K1-1 (underidentified) Ha: matrix has rank=K1 (identified) Kleibergen-Paap rk LM statistic Chi-sq(11)=2.70 P-val=0.9941 Kleibergen-Paap rk Wald statistic Chi-sq(11)=2.68 P-val=0.9943

#### Weak identification test

Ho: equation is weakly identified Kleibergen-Paap Wald rk F statistic 0.084

#### Weak-instrument-robust inference

Tests of joint significance of endogenous regressors B1 in main equation Ho: B1=0 and overidentifying restrictions are valid Anderson-Rubin Wald test  $\rm F(31,1163){=}3.22$  P-val=0.0000 Anderson-Rubin Wald test Chi-sq(31)=103.17 P-val=0.0000 Stock-Wright LM S statistic Chi-sq(31)=86.96 P-val=0.0000

#### Overidentification test of all instruments

Hansen J statistic: 7.445  $Chi-sq(10)$  P-val = 0.6829